

1-4 Practice

Name the property that each statement illustrates.

1. $12 + 917 = 917 + 12$

C.P. of A

2. $74.5 \cdot 0 = 0$

M.P. of Zero

3. $35 \cdot x = x \cdot 35$

C.P. of M.

4. $3 \cdot (-1 \cdot p) = 3 \cdot (-p)$

M.P. of -1

5. $m + 0 = m$

Identity Prop. of Add

6. $53.7 \cdot 1 = 53.7$

I.P. of M.

Use mental math to simplify each expression.

7. $36 + 12 + 4$

52

8. $19.2 + 0.6 + 12.4 + 0.8$

9. $2 \cdot 16 \cdot 10 \cdot 5$

1600

10. $12 \cdot 18 \cdot 0 \cdot 17$

0

Simplify each expression. Justify each step.

11. $6 + (8x + 12)$

18 + 8x

12. $5(16p)$

(5 · 16)p

80p

13. $(2 + 7m) + 5$

14. $\frac{3 \cdot 12st}{At}$

35

$\frac{12}{4} \cdot \frac{8}{1} \cdot \frac{1}{2}$

35 · 1

35

Tell whether the expressions in each pair are equivalent.

15. $7x$ and $7x \cdot 1$

=

16. $4 + 6 + x$ and $4 \cdot x \cdot 6$

10 + x ≠ 24 · x

17. $(12 - 7) + x$ and $5x$

5 + x ≠ 5x

18. $p(4 - 4)$ and 0

p(0) = 0

19. $\frac{124xy}{2x}$ and $12y$

=

20. $\frac{27m}{(3+9-12)}$ and $27m$

12 - 12 = 0

$\frac{27m}{0} \neq 27m$

21. You have prepared 42 mL of distilled water, 18 mL of vinegar and 47 mL of salt water for an experiment.

- How many milliliters of solution will you have if you first pour the distilled water, then the salt water, and finally the vinegar into your beaker?
- How many milliliters of solution will you have if you first pour the salt water, then the vinegar, and finally the distilled water into your beaker?
- Explain why the amounts described in parts (a) and (b) are equal.

1-4 Practice (continued)

Use deductive reasoning to tell whether each statement is *true* or *false*. If it is false, give a counterexample.

22. For all real numbers a and b , $a - b = -b + a$.

$$a + (-b) \quad \text{True; C.P. of A}$$

$$a - b = b - a$$

F

23. For all real numbers p , q and r , $p - q - r = p - r - q$.

$$p + (-q) + (-r) = p + (-r) + (-q) \quad \text{True}$$

$$100 - 1 = 1 - 100$$

$$99 \neq -99$$

24. For all real numbers x , y and z , $(x + y) + z = z + (x + y)$.

$$\frac{m}{m} \cdot n = \frac{n}{n} \cdot m$$

25. For all real numbers m and n , $\frac{m}{m} \cdot n = \frac{n}{n} \cdot m$.

26. **Writing** Explain why the commutative and associative properties don't hold true for subtraction and division but the identity properties do.

27. **Reasoning** A recipe for brownies calls for mixing one cup of sugar with two cups of flour and 4 ounces of chocolate. They are all to be mixed in a bowl before baking. Will the brownies taste different if you add the ingredients in different orders? Relate your answer to a property of real numbers.

Simplify each expression. Justify each step.

28. $(6^7)(5^3 + 2)(2 - 2)$

29. $(m - 16)(-7 \div -7)$

30. **Open-Ended** Provide examples to show the following.

- The associative property of addition holds true for negative integers.
- The commutative property of multiplication holds true for non-integers.
- The multiplicative property of negative one holds true regardless of the sign of the number on which the operation is performed.
- The commutative property of multiplication holds true if one of the factors is zero.